

# Unconventional metallic state in the 2D Hubbard-Wigner lattice

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# Outline

- **Theoretical problem:** Mott vs. Wigner insulators.
- **Experimental problem:** the quarter-filled layered molecular crystals  $\theta$ - $\text{ET}_2\text{X}$ , anomalous metallic properties (low D, correlations, charge order, ...).
- **Long-range Coulomb interaction on a lattice:** the Hubbard-Wigner model.  
→ intermediate anomalous metallic phase
- Future experiments?

SF & J. Merino, Phys. Rev. B 80, 165110 (15 oct 2009)

SF, G. Rastelli, PRB 75, 195103 (2007)

SF, B. Valenzuela and D. Baeriswyl, Synth. Met. 141, 193 (2004)

B. Valenzuela, SF, D. Baeriswyl, PRB 68, 045112 (2003)

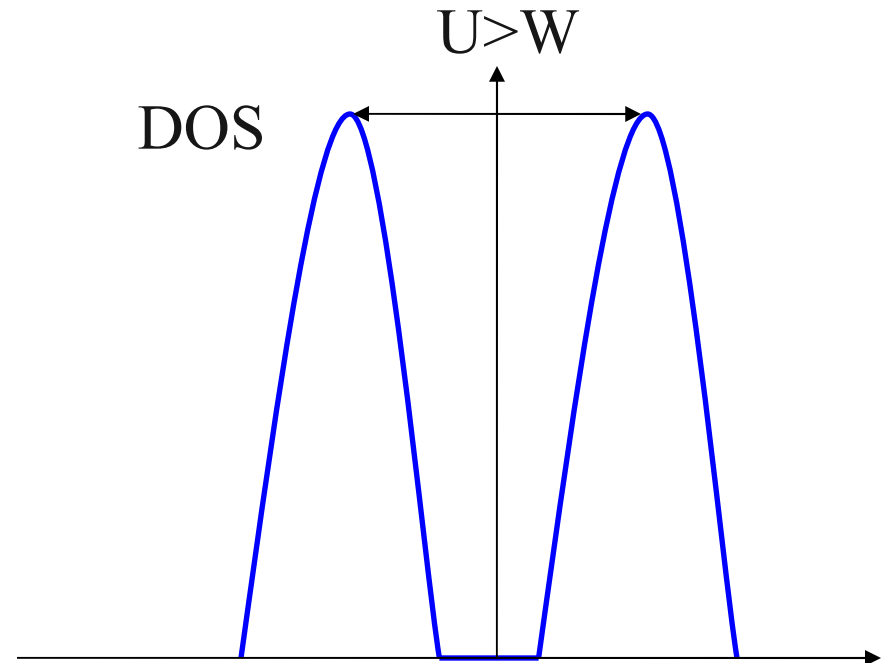
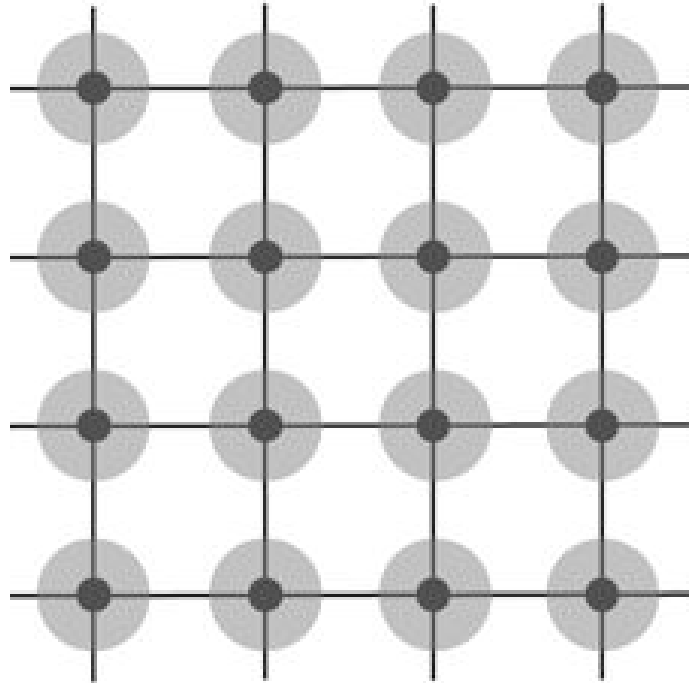
H.Seo, J. Merino, H. Yoshioka, M. Ogata, JPSJ 75, 051009 (2006)

# Mott vs. Wigner insulators

Kinetic energy of electrons is overcome by the Coulomb repulsion energy:  
cuprates, organics, fullerenes,  
manganites, ruthenates,...

→ insulating (localized) due to interactions contrary to predictions of band theory

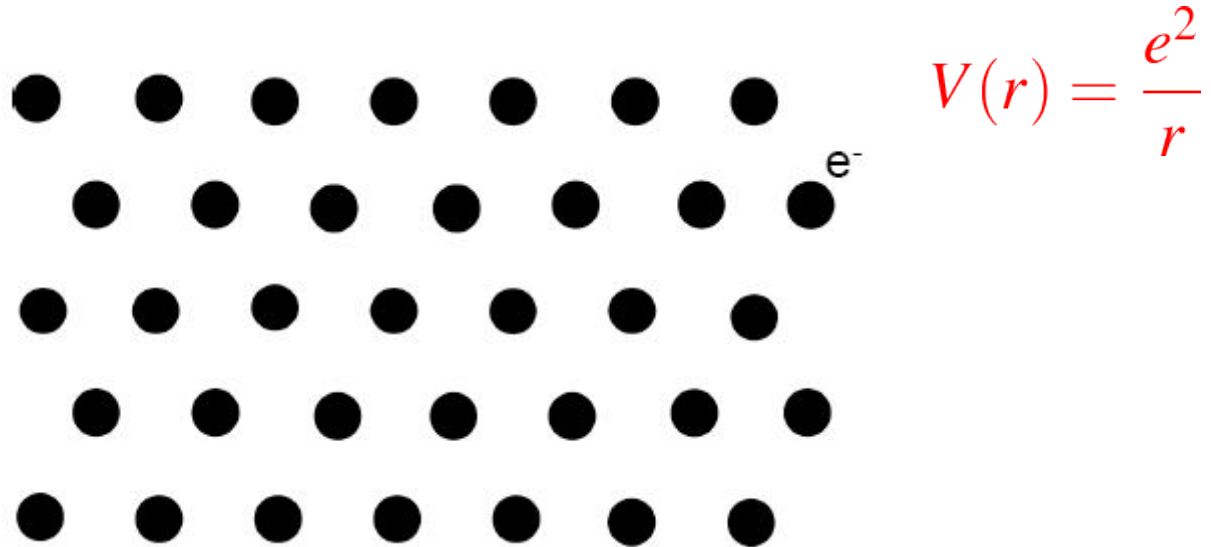
# Mott insulators



- Integer filled bands: cuprates,  $\kappa$ -organics, fullerenes.
- Large on-site Coulomb repulsion,  $U > W$  (bandwidth), on a lattice: d-orbitals, molecular orbitals in a crystal.

# Wigner crystal in a 2D electron gas

## Hexagonal Wigner crystal in 2D



- 2DEG with no underlying crystal lattice.
- At low-density, **long-range** Coulomb repulsion dominates over the kinetic energy, electrons crystallize on a triangular lattice.

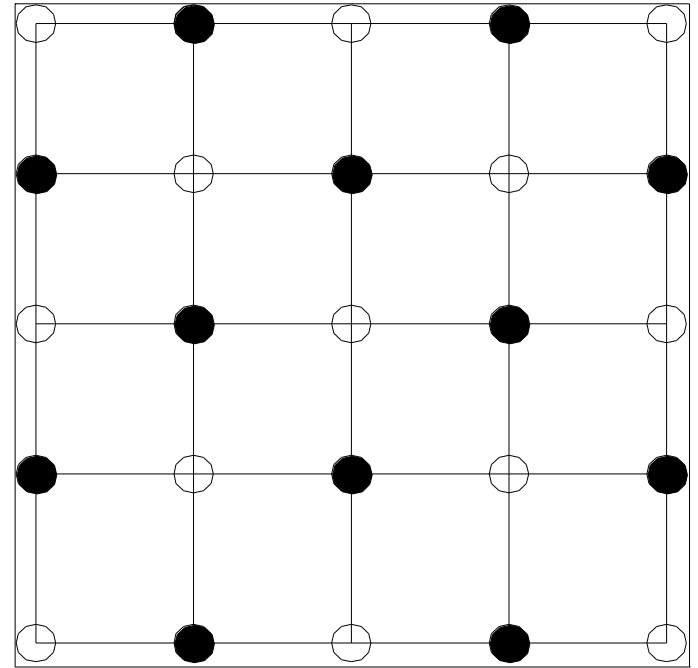
[Wigner (1934)]

# Wigner crystal on a 2D lattice

Simplest example: WC on a square lattice at 1/4-filling

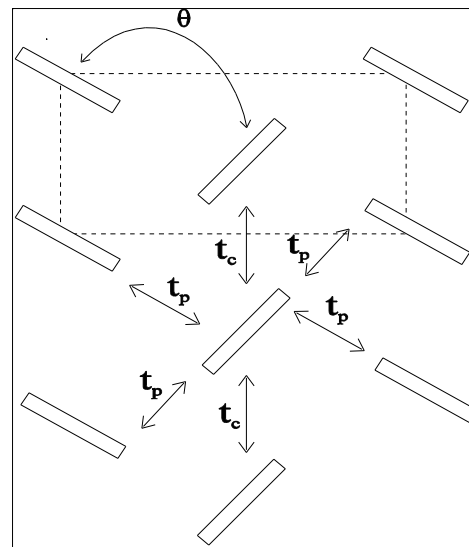
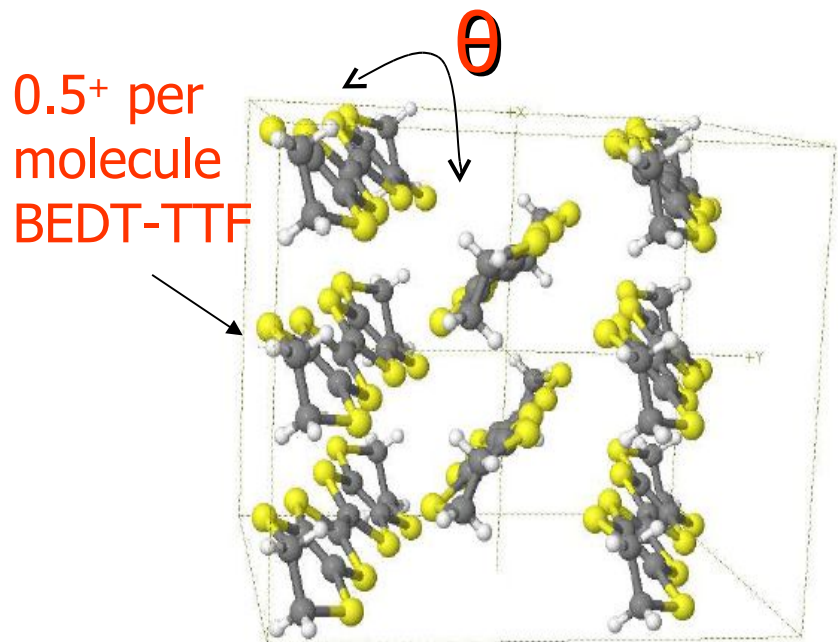
Lattice commensurability localizes electrons on alternating sites instead of the usual triangular arrangement.

[Cocho, EPL, (1986),  
Baeriswyl, Fratini, J. Phys. IV, (2005)]

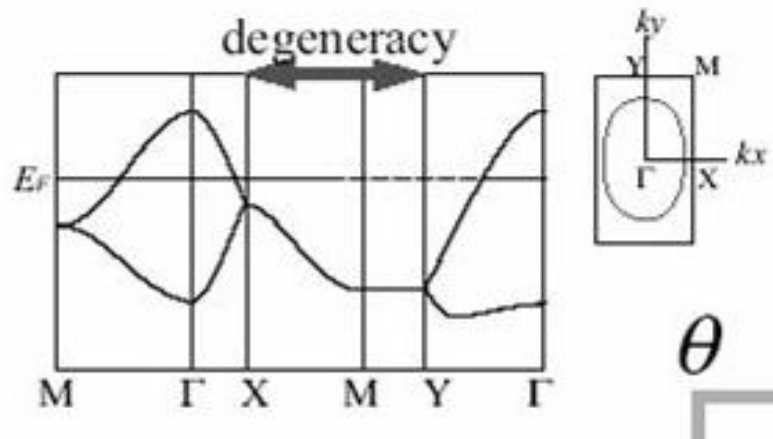


- Wigner crystal physics due to **Long Range** interactions
- Mott physics (electronic correlations) due to **local U**

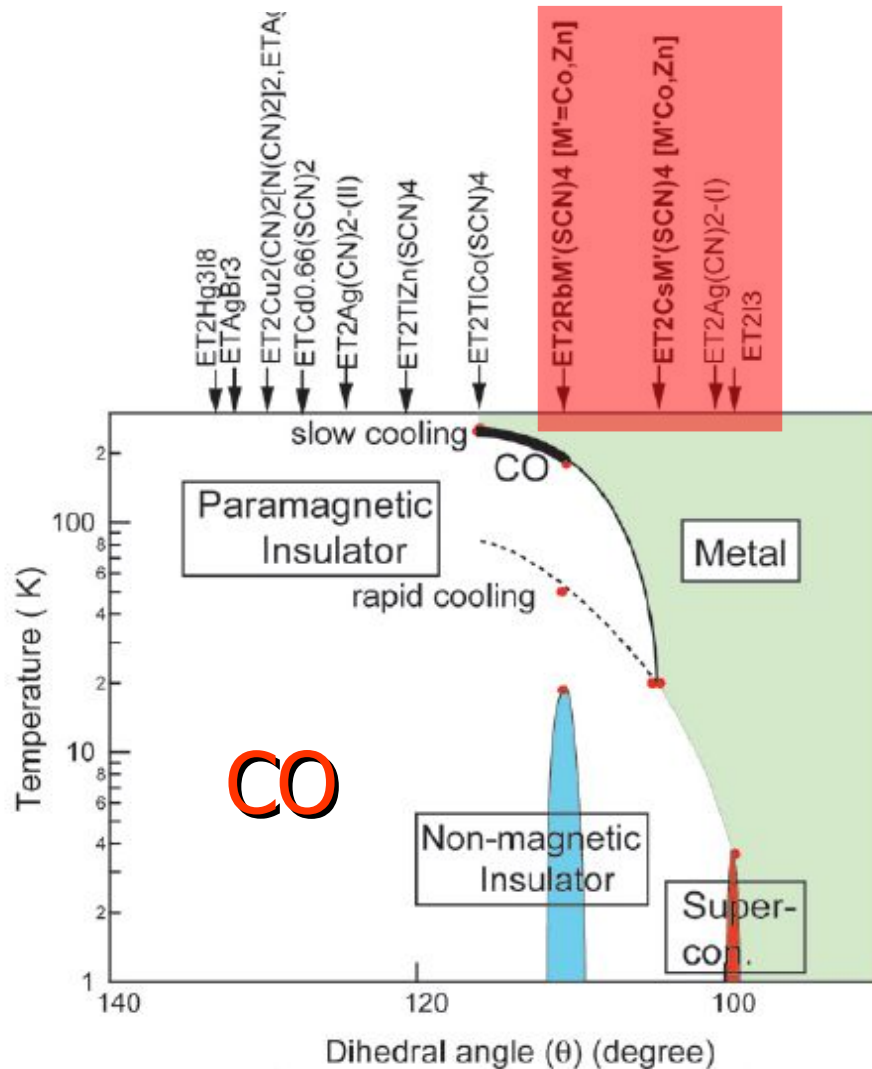
# Organic salts $\theta$ -(BEDT-TTF<sup>0.5+</sup>)<sub>2</sub>X<sup>-</sup>



Tight-binding predicts quarter-filled HOMO bands: metallic state



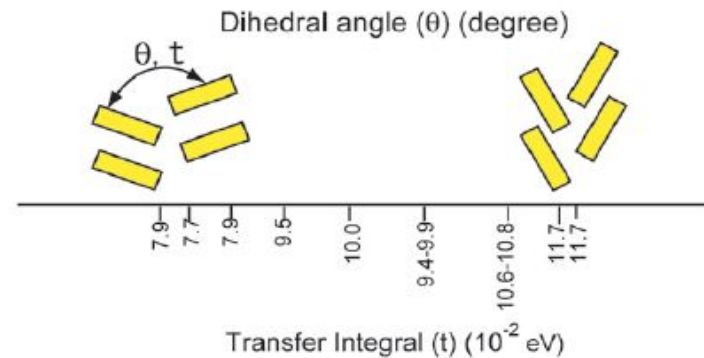
# Phase diagram



[Mori, JPSJ (2006)]

On the verge of metal/CO transition

- large  $U > W$
- bad metal,  $V \sim W$
- poorly screened interactions  $\rightarrow$  long-ranged





# Hubbard-Wigner model

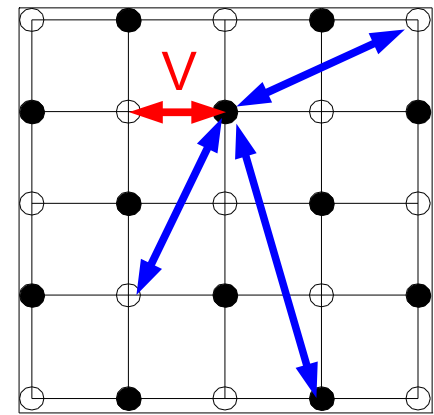
$$\hat{H} = \hat{T} + \hat{U} + \hat{V}$$

$$\hat{T} = -t \sum_{\langle ij \rangle \sigma} c_{i\sigma}^+ c_{j\sigma} + h.c.$$

$$\hat{U} = U \sum n_{i\uparrow} n_{i\downarrow} \quad \text{On-site repulsion}$$

$$\hat{V} = \sum_{i \neq j}^i V_{ij} n_i n_j \quad \text{Non-local repulsion}$$

1/4 filling, square lattice



- Extended Hubbard Model (EHM):  $V_{ij} = V(n.n.)$
- Hubbard-Wigner Model (HWM):  $V_{ij} = \frac{V}{|i-j|}$

both models give charge ordering at  $V > V_{co}$ , **but...**

# $V_{\text{CO}}$ - homogeneous metal to CO transition

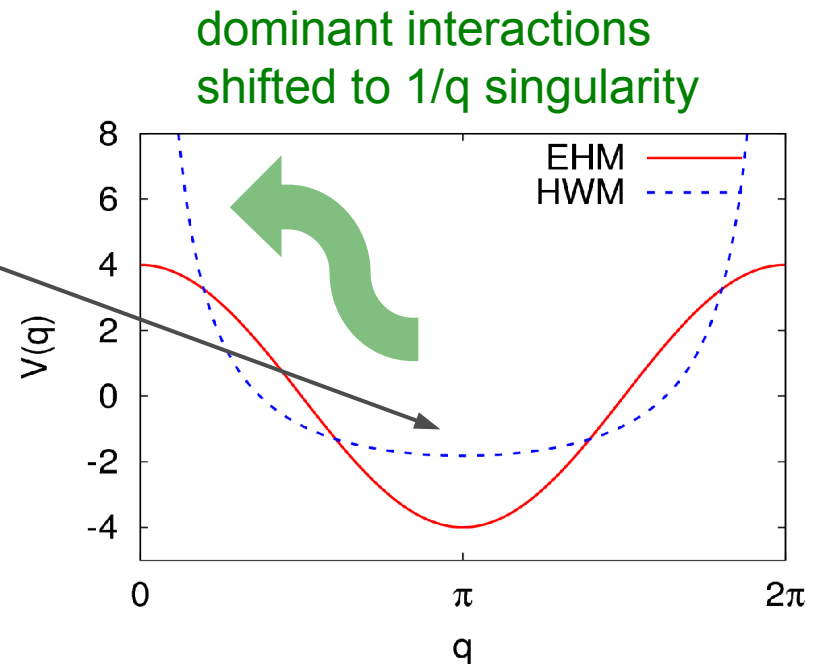
Long range Coulomb interactions stabilize the metallic state (“softer” charge fluctuations).

- RPA charge susceptibility  $Q=(\pi, \pi)$ :

$$\chi_c(\mathbf{Q}) = \chi_0(\mathbf{Q}) / [1 + V(\mathbf{Q})\chi_0(\mathbf{Q})]$$

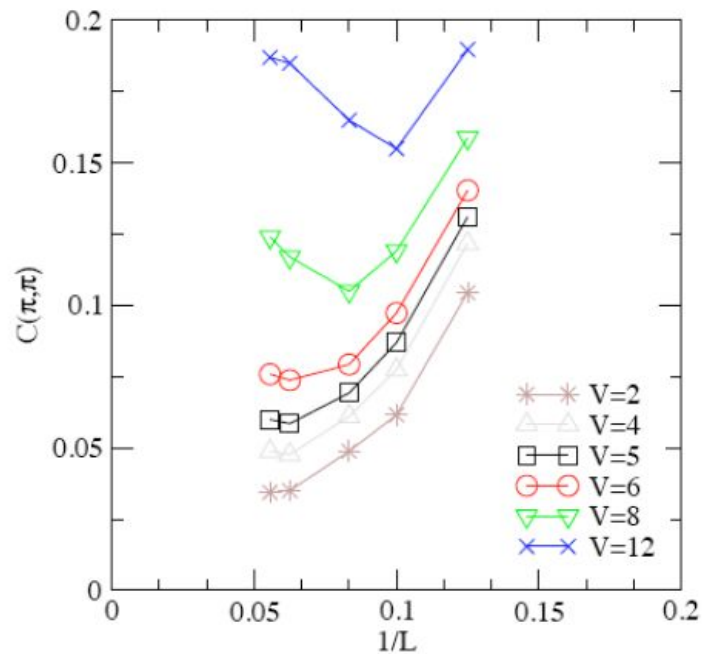
$$\rightarrow V_{\infty}(\text{HWM}) = 2.5 V_{\infty}(\text{EHM})$$

- ED:  $V_{\infty}(\text{HWM})=4t \gg V_{\infty}(\text{EHM})=1.5t$

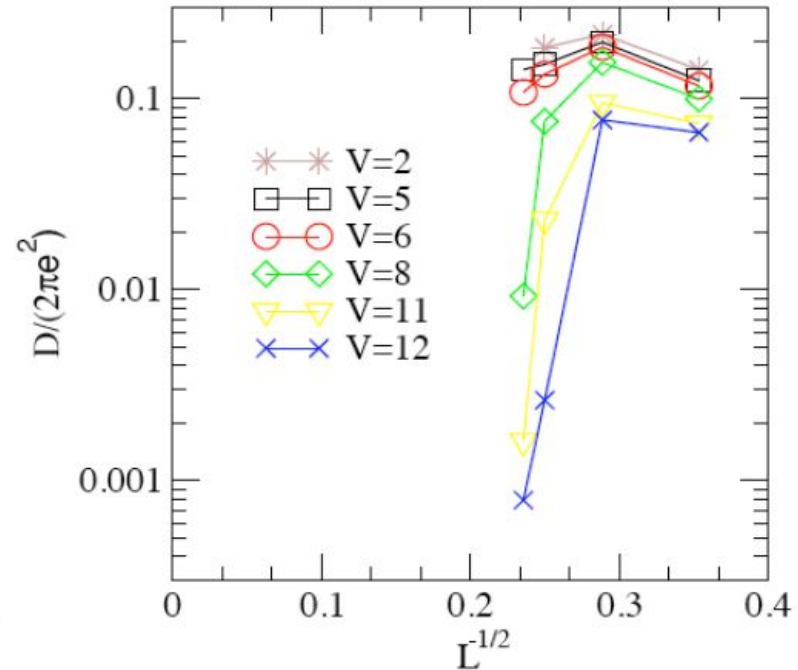


- Explains why compounds are metallic despite nominally large  $V$  and small bandwidths
- yet, the large energy scale  $V$  is still present locally in metallic phase:  
**LR/SR separation, richer physics than in short range models**

# $V_{MI}$ - Metal to Insulator transition $> V_{CO}$



Charge order transition occurs at  $V_{CO} \sim 4t$ . (1.5t if EHM)



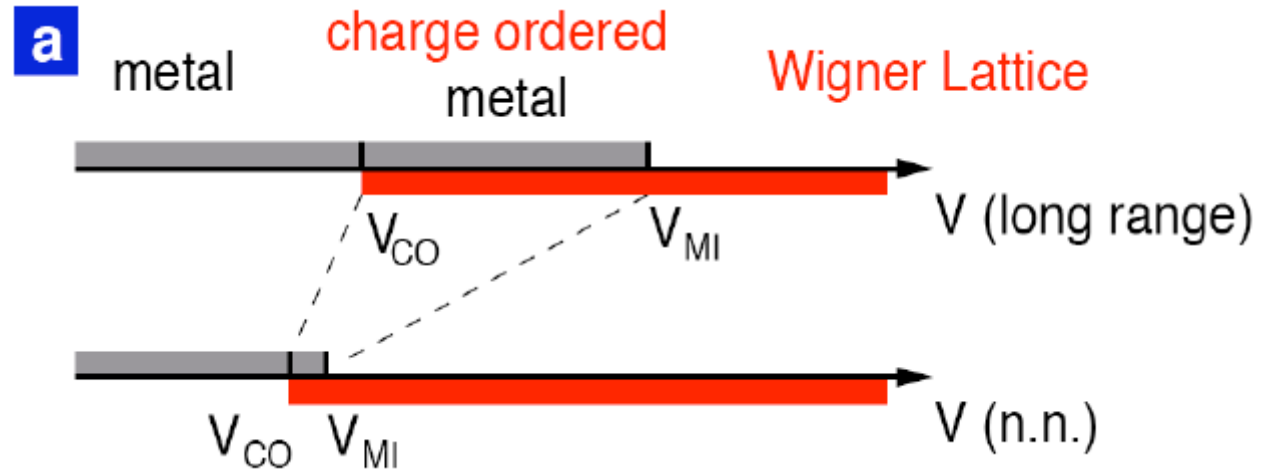
Metal-insulator transition occurs at  $V_{MI} = 8t$

$V_{MI} > V > V_{CO}$  : Intermediate phase separates Wigner crystal from homogeneous metal: charge ordered metallic phase !!!

# Phase diagram from ED

Hubbard-Wigner

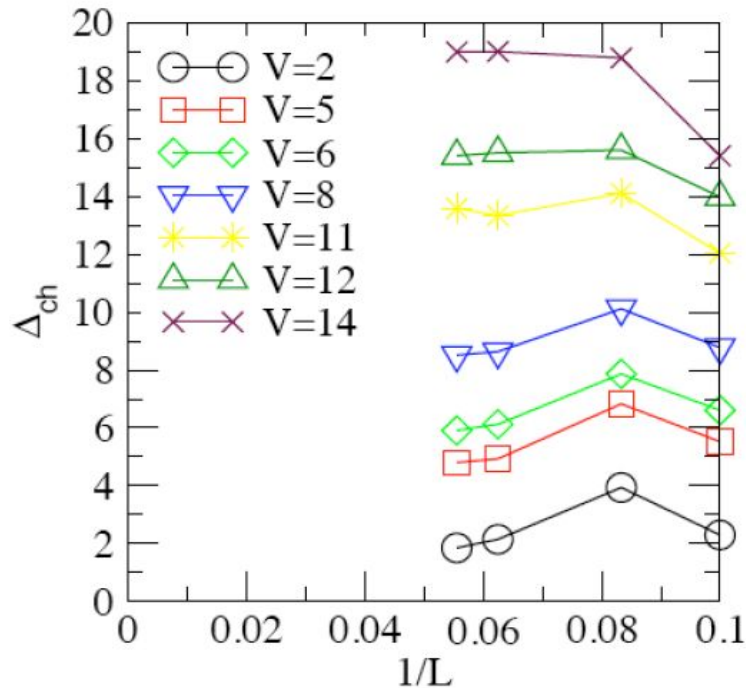
Ext Hubbard



Long range repulsion:

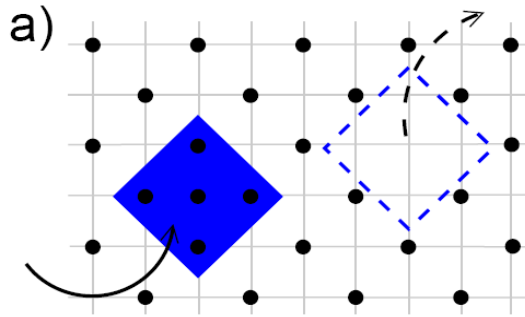
- $V_{CO}$  increases compared to EHM
- Intermediate « strange » phase emerges: CO and metallic

# Charge gap: even more anomalous!

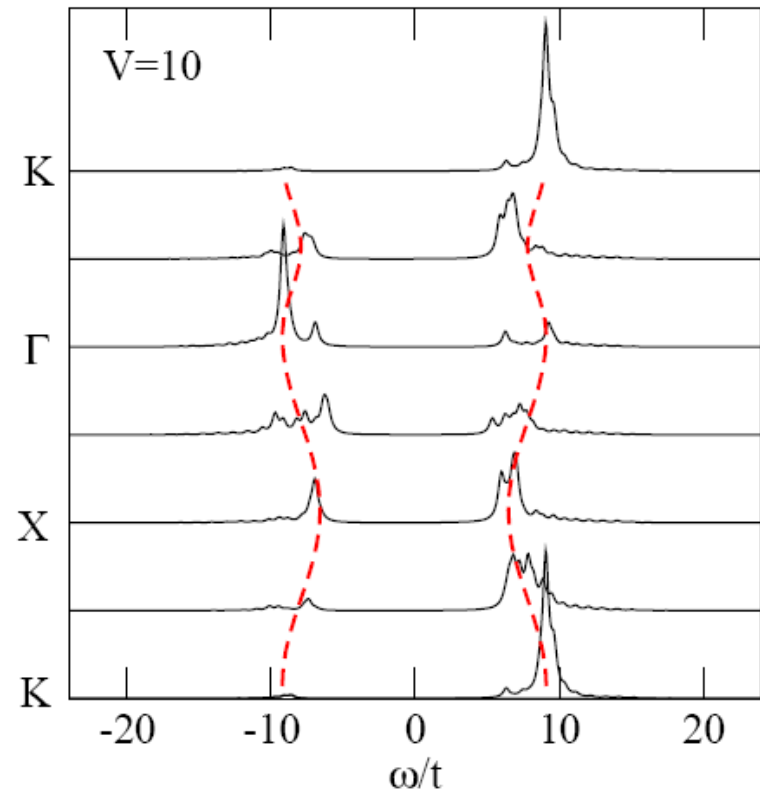


- One-particle (photoemission) charge gap opens up at the CO transition,  $V_{\infty} = 4-5t$ .
- Metallic phase without DOS at the Fermi energy for  $V_{\infty} < V < V_{\text{MI}}$  !  
→ who carries the current? collective excitations?

# Collective excitations, large $V/t$ limit: charged (photoemission)



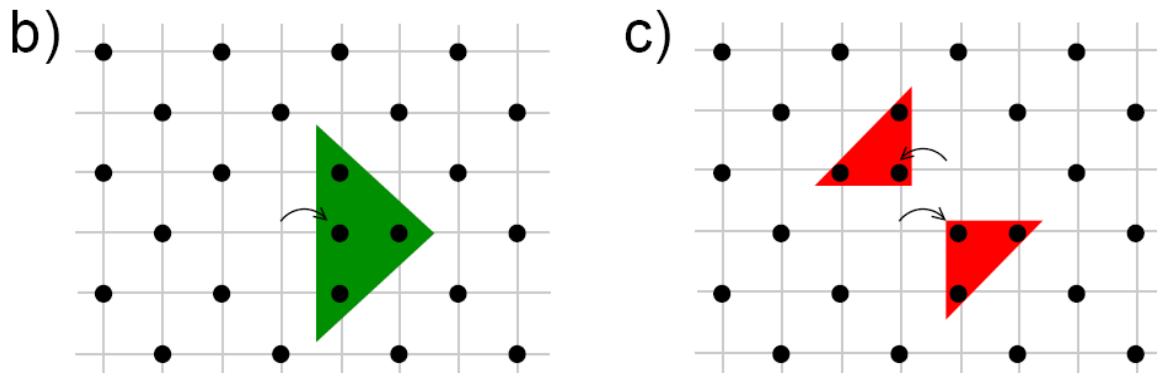
$$E_k = E_0 - 2t_1[\cos(2k_x) + \cos(2k_y)] - 2t_2[\cos(k_x + k_y) + \cos(k_x - k_y)].$$



“Pinball liquid” (cf. Hotta, Furukawa)  
charges flowing on top of an underlying CO pattern, pin/ball separation

# Collective excitations: charged (sails and butterflies) $\sigma(\omega)$ , $\epsilon$

dipolar, quadrupolar



$$\Delta_{dp} = 3V$$

$$\Delta_{dp} = 0.62V$$

← Extended Hubbard

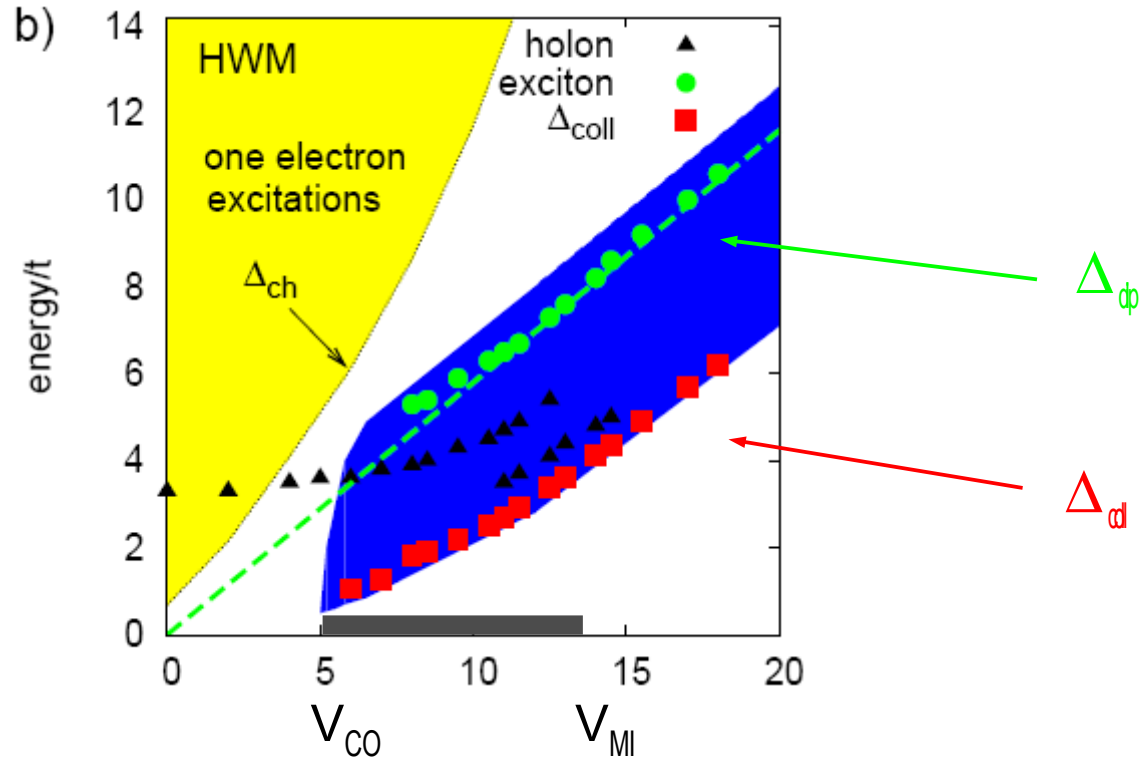
← Hubbard-Wigner

$$\rightarrow \Delta_{qed} = 4V$$

$$\rightarrow \Delta_{qed} = 0.65V$$

“Electrostatic frustration”: large degeneracy due to long range  
Coulomb interaction leads to delocalization of defects!

# Collective excitations: ED



- Defects gain kinetic energy  $\propto t$ , by deconfinement.

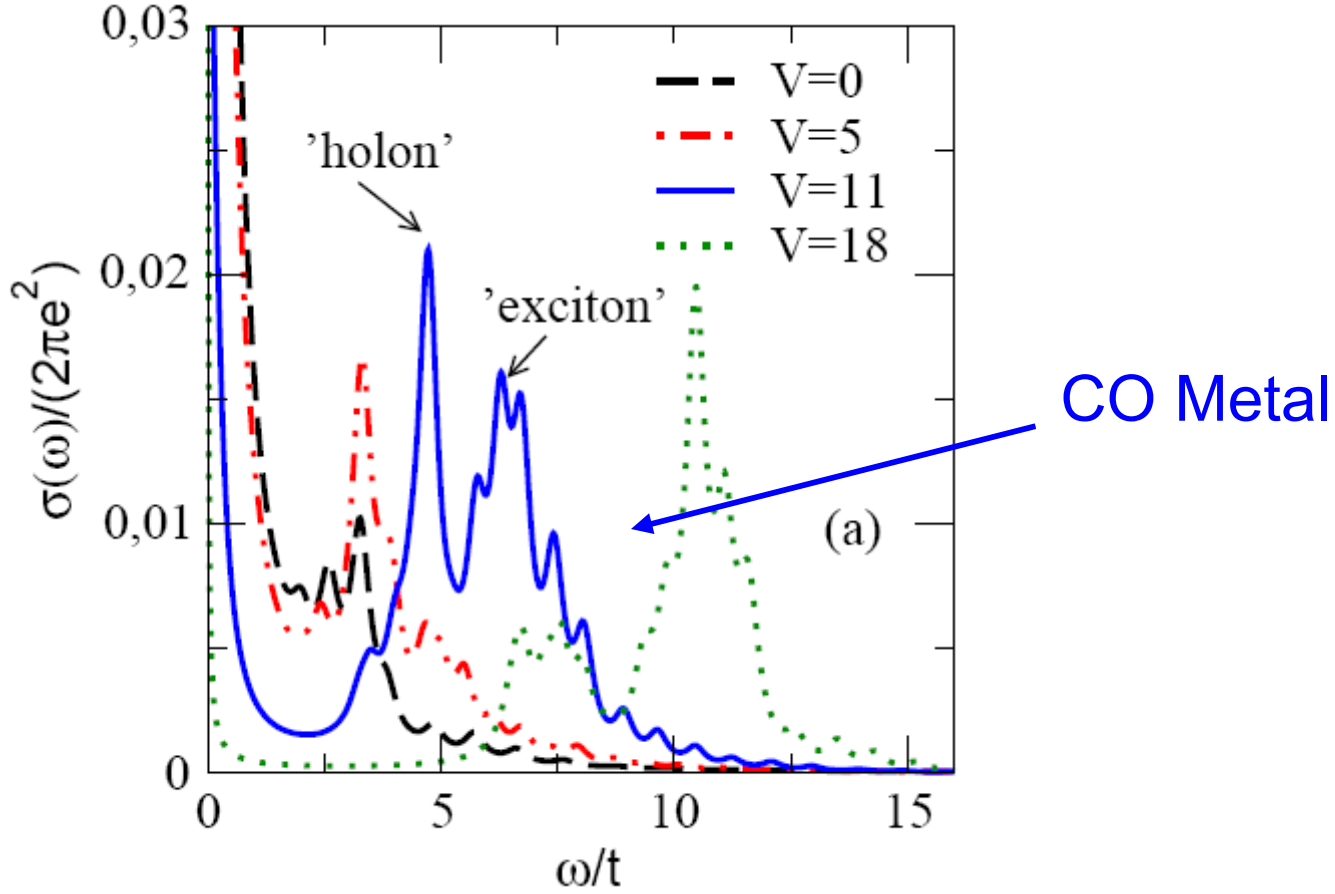
$$\Delta_d = \Delta_{\phi p} - 4.2t. \quad [\text{only } \sim t^2/V \text{ in EHM}]$$

- Defects drive the transition to the anomalous phase, as they dominate the low energy behavior close to  $V_{MI}$  (cf. 1D case)
- Their precise nature is unknown (mixing with “Mott” collective excitations)



# Optical conductivity in the anomalous phase

Both features related to Mott correlated metal and Wigner crystal



# Conclusions

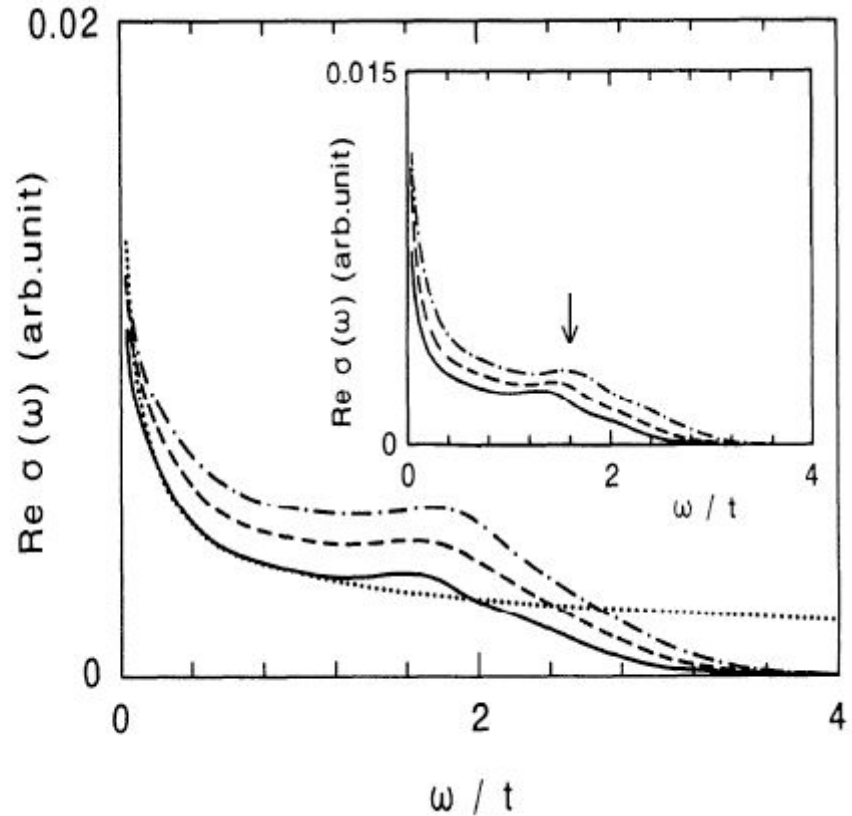
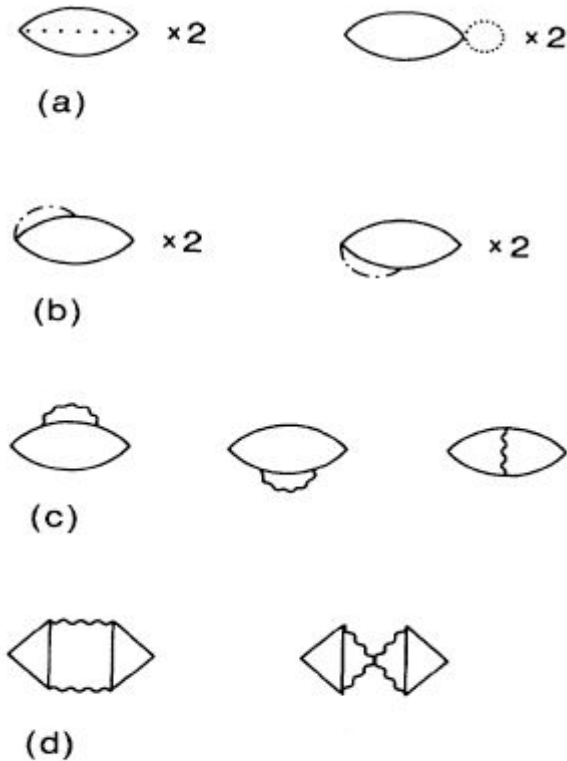
- Anomalous metallic state with Wigner crystal charge order AND Mott correlations occurs in phase diagram of 2D Hubbard-Wigner model:
  - Drude peak is non-zero signalling a metallic state.
  - One-electron excitations display a gap → collective modes
  - Delocalized defects due to long range Coulomb repulsion are responsible of current flow despite the charge gap.
- Key experiments:
  - Optical spectroscopy should observe a Drude peak and excitonic + “holon” band.
  - Photoemission experiments should observe a charge gap.
  - X-ray, NMR, should observe charge ordering

# Relevance to organics: $\theta$ -(BEDT-TTF)<sub>2</sub>X

Quarter-filled organics are ideal systems for exploring the quantum melting of a Wigner crystal on a lattice (tunable  $V/t$ )

- $X=I_3$  is a correlated metal, with no visible Drude peak and resistivity well beyond the Mott-Ioffe-Regel limit [Takenaka PRL (2005)]
- $X=RbZn(SCN)_4$  salt displays a CO transition at  $T_\infty = 195$  K.
  - Resistivity has a **metallic behavior for  $T > T_\infty$** .
  - **Short range ordering** found by NMR for  $T > T_\infty$ . [Chiba PRL (2004)]
  - Thermopower shows **both localized and mobile carriers** [Abdel-Jawad PRB (2009)]
  - STM/STS finds (?) a large gap of 0.6 eV for  $T < T_\infty$   
Even above  $T_\infty$  a small gap of about 0.1 eV is observed.  
[Ichimura JLTP (2009)].
- $X=CsZn(SCN)_4$  salt displays nonlinear resistivity ascribed to collective excitations [Inagaki JPSJ (2004), Sawano Nature (2005)]

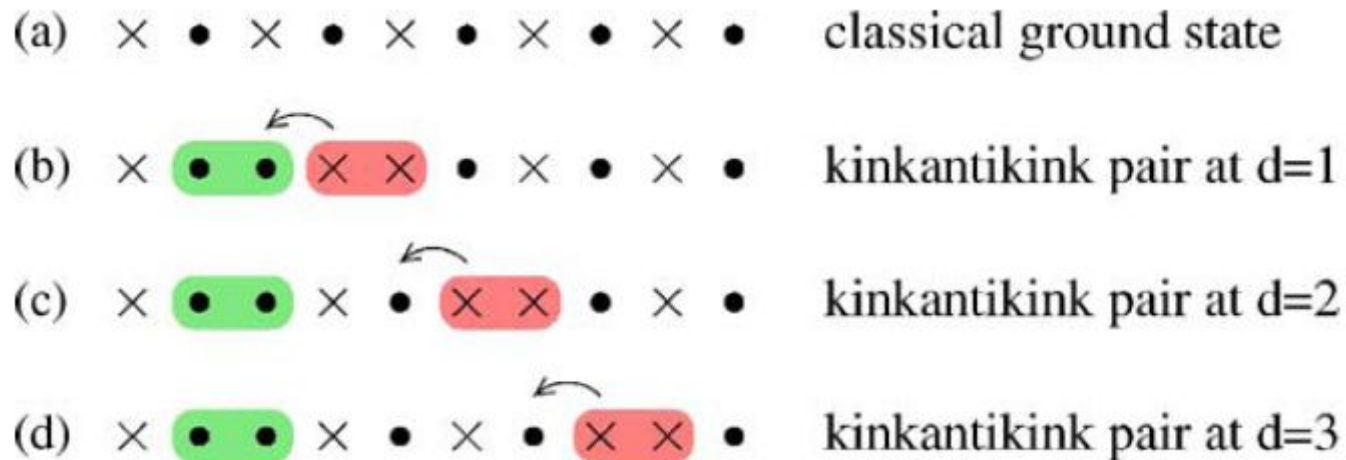
# 'Holon' in strongly correlated 2D metal



Large-N theory of 't-J' model: **Bang & Kotliar, PRB (1993).**

# Wigner crystal on a 1D chain: collective excitations and charge fractionalization

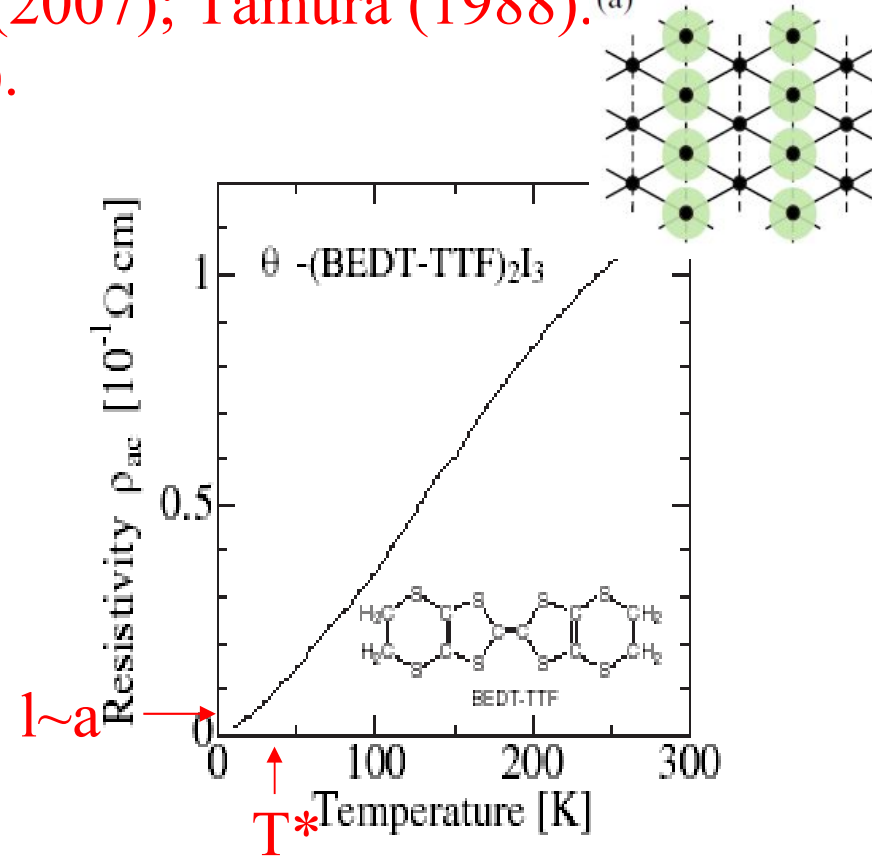
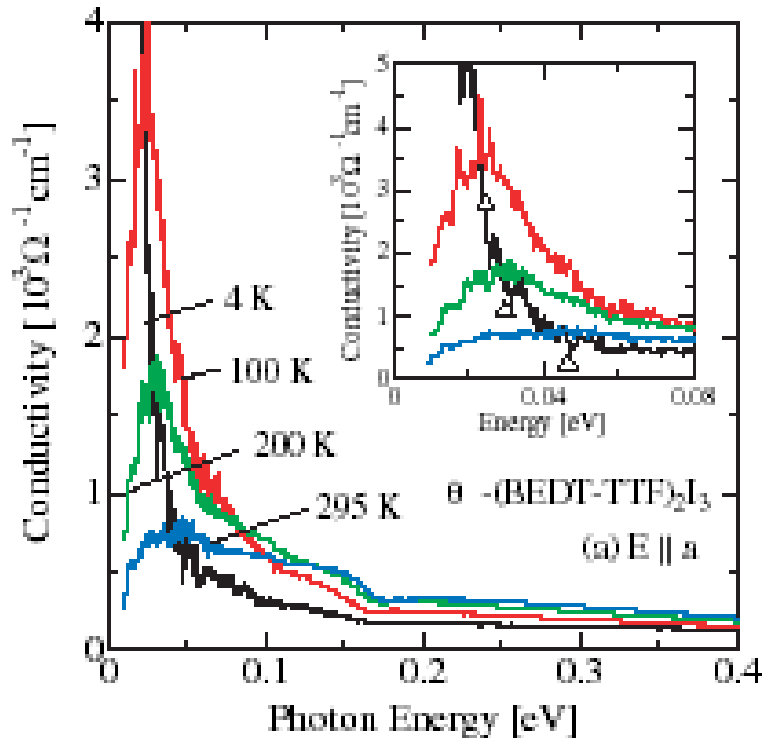
J. Hubbard, PRB (1978), Fratini et. al., Synth. Met. (2004),  
Mayr and Horsch, PRB (2006).



The degeneracy of the classical ground states leads to the formation of domain walls of fractional charge.

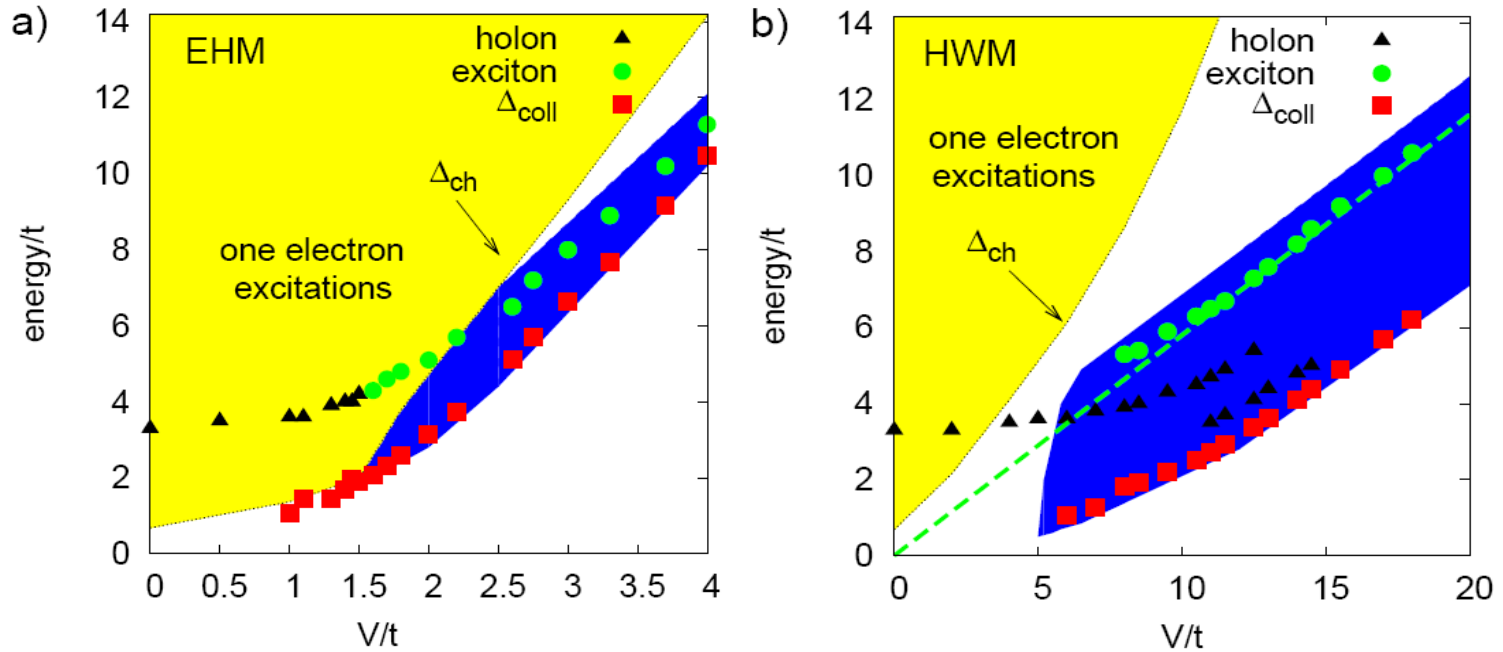
# Correlated metal: $\theta$ -(ET)<sub>2</sub>I<sub>3</sub>

Takenaka, et. al., PRL (2005); PRL (2007); Tamura (1988).<sup>(a)</sup>  
Gunnarsson and Vafayi, PRL (2007).



- No visible Drude peak at  $T > 4$  K.
- Metallic resistivity increases above the Mott limit  $T > 50$  K.

# Collective excitations: HWM vs EHM



- In the EHM, the transition occurs when  $\Delta_{\phi} \sim W \rightarrow V/t \sim 2$
- In the HWM defects gain kinetic energy  $\propto t$ , by deconfinement and remain as the low energy sector down to the transition.

$$\Delta_d = \Delta_{\phi} - 4.2t. \quad [\text{only } \sim t^2/V \text{ in EHM}]$$