# Kapellasite: un liquide de spin sur kagome avec des interactions en compétition

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Band theory  $\rightarrow$  the Mott insulators are conducting  $!\dots$ 

The Hubbard model integrates interactions between electrons:

$$H_{Hub} = t \sum_{\langle ij \rangle, \sigma = \pm 1/2} c^{\dagger}_{i\sigma} c_{j\sigma} + \frac{U}{\sum_{i}} \underbrace{n_{i\uparrow}}_{c^{\dagger}_{i\uparrow}} c_{i\uparrow} n_{i\downarrow}.$$





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To  $2^{nd}$  order in perturbation theory in  $\frac{t}{U}$ :

$$H = \frac{4t^2}{U} \sum_{\langle ii \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$
 (Heisenberg model).





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To  $2^{nd}$  order in perturbation theory in  $\frac{t}{U}$ :

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Frustration  $\Rightarrow$  spin liquids

## Perfect S = 1/2 kagome compounds

Herbertsmithite (see F. Bert's talk) Zn-paratacamite  $Cu_3Zn(OH)_6Cl_2$ 

#### Kapellasite

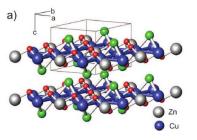
Polymorph of Herbertsmithite,

R. H. Colman et al, Chem. Mater. 20 6897 (2008)

#### Important $J_d$ interaction

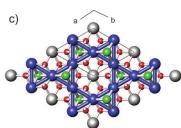
O. Janson et al, PRL  $101\ 106403\ (2008)$ 

#### 2D behaviour



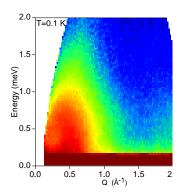


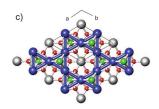




## **Experiments on kapellasite**

- $\qquad \mathsf{NMR} \to (\mathsf{Cu}_{0.73}\mathsf{Zn}_{0.27})_3(\mathsf{Zn}_{0.88}\mathsf{Cu}_{0.12})(\mathsf{OH})_6\mathsf{Cl}_2,$
- lacktriangle Magnetic susceptibility and  $\mu$  SR ightarrow gapless spin liquid state,
- ► Inelastic neutron scattering:

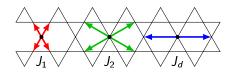




- No Bragg peak → no long range order.
- No gap
- ▶ Intensity around  $0.5A^{-1}$



## High temperature series analysis

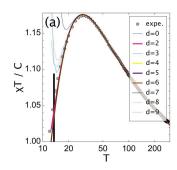


#### Analysis of

- the magnetic susceptibility,
- the low temperature specific heat data

#### Results for kapellasite:

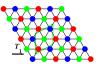
- ►  $J_1 = -12K$  (F),
- ►  $J_2 = -4K$  (F)
- $J_d = 15.6K \text{ (AF)}$



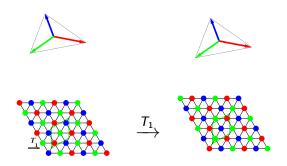
B. Bernu, C. Lhuillier, E. Kermarrec, F. Bert, P. Mendels, R. H. Colman, A. S. Wills, PRB 87 155107 (2013)

#### Example:

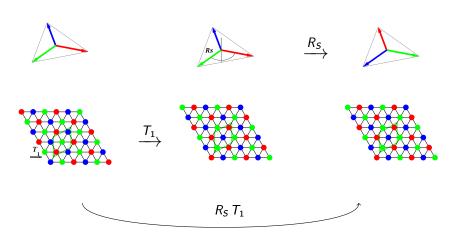




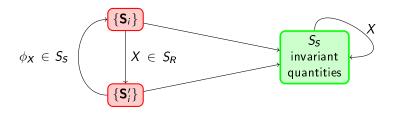
Example: This state is not invariant by the translation  $T_1$ ,



Example: This state is not invariant by the translation  $T_1$ , but it is by  $T_1$  followed by a global spin rotation  $R_S$ .



We know the lattice and its symmetries  $S_R$ , the spin space and its symmetries  $S_S$ .



#### Definition:

A classical state is *regular* for the lattice symmetry X if there is a global spin transformation  $\phi_X$  such that the state is unchanged by  $\phi_X X$ .

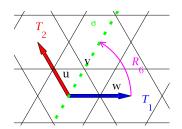
LM, Lhuillier and Misguich, PRB 83, 184401 (2011)



## How to find the regular states?

The research consists in two steps.

Example of the kagome lattice with Heisenberg spins

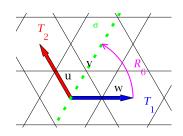


## How to find the regular states ?

The research consists in two steps.

(1) Find the  $\phi_X$  from  $S_S$  respecting the algebraic structure of  $S_R$ ,

## Example of the kagome lattice with Heisenberg spins



(1) Algebraic constraints on  $\phi_X$  from O(3):

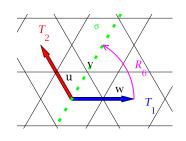
$$\begin{split} \phi_{T_{1}}\phi_{T_{2}} &= \phi_{T_{2}}\phi_{T_{1}} & \phi_{T_{1}}\phi_{R_{6}}\phi_{T_{2}} = \phi_{R_{6}} \\ \phi_{R_{6}}\phi_{\sigma}\phi_{R_{6}} &= \phi_{\sigma} & \phi_{T_{1}}\phi_{\sigma} = \phi_{\sigma}\phi_{T_{2}} \\ \phi_{R_{6}}^{6} &= I & \phi_{\sigma}^{2} &= I \\ \phi_{R_{6}}\phi_{T_{1}}\phi_{T_{2}} &= \phi_{T_{2}}\phi_{R_{6}}. \end{split}$$

## How to find the regular states?

The research consists in two steps.

- (1) Find the  $\phi_X$  from  $S_S$  respecting the algebraic structure of  $S_R$ ,
- (2) For each set of  $\phi_X$ , find the compatible states.

Example of the kagome lattice with Heisenberg spins



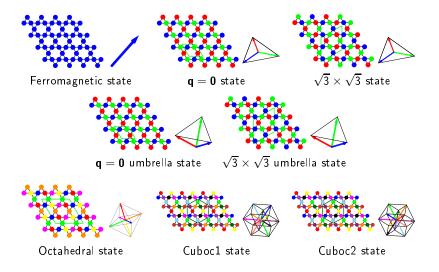
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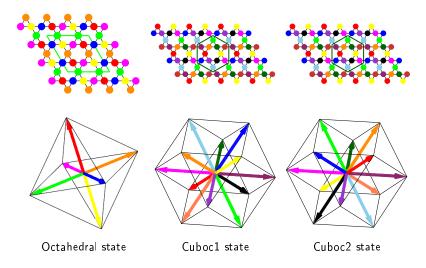
(2) Constraints on the spin state:

$$\phi_{\sigma} \mathbf{S}_{\nu} = \mathbf{S}_{\nu}, \qquad \phi_{T_{1}} \phi_{T_{2}} \phi_{R}^{3} \mathbf{S}_{\nu} = \mathbf{S}_{\nu}.$$

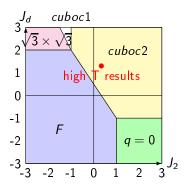
## Regular states on the kagome lattice



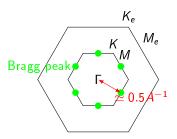
## Regular chiral states on the kagome lattice



## Classical phase diagram for $J_1 = -1$



Structure factor of cuboc2



The low T phase in kapellasite is a spin liquid with short range correlations similar to the cuboc2 state  $\rightarrow$  chiral spin liquid

How to theoretically describe this phase ?

## Theoretical description

In spin liquids, excitations are fractional quasiparticles: spinons (S = 1/2).

- ▶ bosonic description → Néel phases and gapped spin liquids,
- ▶ fermionic descrition  $\rightarrow$  gapped and non gapped spin liquids. (work in progress with Samuel Bieri).

In both cases, all spin liquid phases can be listed using the projective symmetry group approach (Wen, 2002), and fluxes can be calculated and used to identify similar phases obtained through different approaches.

Taking into account chiral spin liquids is something new and leads to still unexplored phases!

#### Thanks to

#### For the synthesis

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- F. Bert (LPS, Orsay),
- P. Mendels (LPS, Orsay),
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- A. Amato (LMU, PSI, Switzerland),

#### For the theory

- B. Bernu (LPTMC, Paris),
- C. Lhuillier (LPTMC, Paris),
- S. Bieri (LPTMC, Paris),



## The Schwinger boson mean-field theory (SBMFT)

On each site j, bosons with spin  $1/2 \uparrow (\downarrow)$  are created by  $a_i^{\dagger} (b_i^{\dagger})$ .

$$2S_{j}^{z} = a_{j}^{\dagger}a_{j} - b_{j}^{\dagger}b_{j}, \qquad S_{j}^{+} = a_{j}^{\dagger}b_{j}, \qquad n_{j} = 2S$$

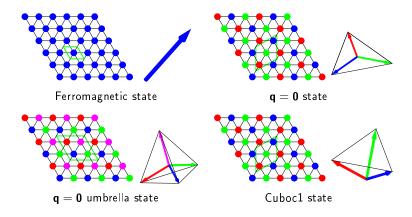
 $\widehat{A}_{ij} = \frac{1}{2} (a_i b_j - b_i a_j) = \text{rotationally invariant bond operator}$ 

$$\widehat{A}_{ij}^{\dagger}\widehat{A}_{ij} \rightarrow \textit{MF} \rightarrow \langle \widehat{A}_{ij}^{\dagger} \rangle \widehat{A}_{ij} + \langle \widehat{A}_{ij} \rangle \widehat{A}_{ij}^{\dagger} - |\langle \widehat{A}_{ij} \rangle|^2$$

Average number of bosons adjusted to be  $\kappa$  (real) :

$$a_i^{\dagger} a_i + b_i^{\dagger} b_i = 2S \rightarrow \langle a_i^{\dagger} a_i + b_i^{\dagger} b_i \rangle = \kappa.$$

## Regular states on the triangular lattice



### Regular states on the square lattice

